# Statistical Method for Predicting When Patients Should Be Ready on the Day of Surgery 

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#### Abstract

Background：Previously，mathematical theory was developed for determining when a patient should be ready for surgery on the day of surgery．To apply this theory，a method is needed to predict the earliest start time of the case． Methods：The authors calculated a time estimate such that the probability is 0.05 that the preceding case in the patient＇s op－ erating room（OR）will be finished before the patient is ready for surgery．This implies there will be a $5 \%$ risk of OR personnel being idle and waiting for the patient．This 0.05 value was chosen by considering the relative cost valuation of an average patient＇s time to that of an average surgical team based on national salary data．Case duration data from a surgical services information system were used to test different statistical meth－ ods to estimate earliest start times． Results：Simulations found that 0.05 prediction bounds，cal－ culated assuming case durations followed log－normal distribu－ tions，achieved actual risks for the OR staff to wait for patients of 0.050 to 0.053 （SEM $=0.001$ ）．Nonparametric prediction bounds performed no better than the parametric method．Hav－ ing patients ready a fixed number of hours before the sched－ uled starts of their operations is not reliable．If the preceding case in an OR had been underway for 0.5 to 1.5 h ，the paramet－ ric 0.05 prediction bounds for the time remaining achieved actual risks for OR staff waiting of 0.055 to 0.058 （SEM $=0.001$ ）． Conclusion：The earliest start time of a case can be estimated using the 0.05 prediction bound for the duration of the preced－ ing case．The authors show 0.05 prediction bounds can be estimated accurately assuming that case durations follow log－ normal distributions．（Key words：Operating room manage－ ment；operating room scheduling；perioperative scheduling．）


WHAT should be a surgical suite＇s policy for telling a patient at what time the patient should arrive at the surgical suite on the day of surgery？Although each surgical case typically has a scheduled start time，it is not clear if the patient should be told to arrive at the surgical suite 2 h before this scheduled start time，or if some longer or briefer length of time would be more appro－ priate．There are three facets to this question．First，will the patient arrive punctually？Second，once the patient has arrived at the surgical suite，how much time will be

[^0]required for the patient to be prepared for surgery（e．g．， to change into a hospital gown and receive medica－ tions）？Third，will the preceding case or cases in the operating room（OR）in which the patient is to have surgery finish early，on time，or late？Provided the patient has already undergone preoperative evaluation，${ }^{1,2}$ the facet resulting in the greatest likelihood of a long patien ${ }^{\frac{5}{2}}$ waiting time on the day of surgery is the variability in the duration of the preceding case or cases．${ }^{3}$
Ideally，a patient would arrive at the surgical suite，b b prepared for surgery，and be ready for surgery just as th preceding case in his or her OR is completed．${ }^{4}$ The patient would then have the short waiting time he or she wants．${ }^{1,5-7}$ In addition，the OR staff would not incur idle巛 time waiting for the patient．In this context，the＂staff $\frac{8}{3}$ include one or more surgeons，anesthesiologists，nurses．${ }_{\text {² }}^{\text {² }}$ and OR technicians．However，if the patient is reade earlier than the time at which the preceding case in hi窓 or her OR finishes，then the patient will incur some waiting time while the preceding case is completed an $\stackrel{\text { B }}{\substack{ \\~}}$ the room is cleaned．This patient will likely be les皆 satisfied．${ }^{1,5-7}$ In contrast，if the patient arrives after the completion of the preceding case in his or her OR，th $\stackrel{\rightharpoonup}{\otimes}$ staff working in the OR will have to wait for the patient
Weiss showed that the determination of when to havè patients arrive on the day of surgery is equivalent tờ specifying quantitatively the relative cost of patients waiting time compared with the cost of the staff＇s idle time．${ }^{4}$ The logic is，in effect，that if there is a high cost fo $\overrightarrow{8}$ some undesired activity，then the probability of that activity occurring should be made as low as possible．Fo g example，at some surgical suites the cost of the staff＇${ }^{\circ}$ idle time is considered to be large relative to the cost $\frac{0}{5}$ the patients＇waiting time．At such surgical suites，the probability of having the OR staff wait for the patien ${ }^{\circ}$ should be made low by having the patients arrive earlyz The surgical suite could implement this policy by in ${ }^{\frac{\circ}{2}}$ structing all patients to stop eating and drinking at mide night and arrive sufficiently early in the morning to be ready for surgery at the start of the regularly scheduled OR day．${ }^{5}$ As a result of the policy，patients who are not scheduled for the first case in each OR have a long waiting time，are thirsty，and can be dissatisfied with their care．${ }^{1,5-7}$ However，the policy ensures that staff working in the surgical suite virtually never wait for patients．
Weiss showed how，in theory，a surgical suite should determine when a patient should be ready for surgery on the day of surgery．${ }^{4}$ Based on the surgical suite＇s relative
valuation ${ }^{1}$ of patients＇waiting time to staff＇s idle time， each patient should be ready for surgery some optimal number of hours before the scheduled end of the pre－ ceding case in the patient＇s OR．Weiss showed that these values need to be estimated，but did not investigate how to calculate them．${ }^{4}$ Our goal was to use actual data from a surgical suite to test different statistical methods that can be used to estimate the earliest start time of a case so that Weiss＇theory can be implemented in surgical suites．

## Methods

## Review of the Previously Developed Theory for Determining When a Patient Sbould Be Ready on the Day of Surgery

Weiss ${ }^{4}$ showed that there is an optimal method for balancing the cost of a patient waiting for the preceding case in his or her OR to be completed with the cost of OR staff waiting for the patient．Let us suppose that the cost of the patient waiting equals $\mathrm{C}_{\mathrm{pt}}$ per hour．The cost of the OR staff waiting for the patient，once the staff have finished caring for the preceding patient in the OR， equals $C_{\text {OR }}$ per hour．The expected total cost for patient and staff waiting equals the number of hours the patient waits multiplied by $\mathrm{C}_{\mathrm{pt}}$ plus the number of hours the OR staff wait multiplied by $\mathrm{C}_{\mathrm{OR}}$ ．Weiss showed that to min－ imize this expected total cost，the time that the patient should be available for surgery is the $\tau$ th percentile of the cumulative distribution function of the duration of the preceding case in the patient＇s OR，where $\tau=$ $\mathrm{C}_{\mathrm{pt}} /\left(\mathrm{C}_{\mathrm{OR}}+\mathrm{C}_{\mathrm{pt}}\right) .{ }^{4}$ To minimize the expected total cost for patient and staff waiting，the risk that the OR staff should accept in having to wait for the patient equals $\tau .{ }^{4}$ For example，suppose that $\tau=0.05$ and the preceding case in the OR is a cholecystectomy．Then，the patient would be asked to arrive sufficiently early so that he or she can be ready for surgery at the time that corresponds to the 0.05 percentile of the durations of cholecystecto－ mies performed at the surgical suite．There would be a 0.05 chance that the OR staff would finish the cholecys－ tectomy and have to wait for the next patient．

We give an example of how these principles ${ }^{4}$ would be applied to determine when a patient whose case is preceded by a cholecystectomy should be ready for surgery．Figure 1 shows a histogram of the durations of the 552 cases scheduled to be a cholecystectomy in the data set（described in Case Duration Data Used in this Study）．The data are plotted with a logarithmic axis．A normal distribution curve，with its characteristic bell shape，is superimposed．The 0.05 percentile of case duration，which equals 1.7 h ，is marked with an arrow． When determining when to have the second patient in the OR be ready for surgery，the duration of the chole－ cystectomy could be expected to be 1.7 h ．By having the second patient available for surgery 1.7 h after the start of the cholecystectomy，the risk of the OR staff having to


Fig．1．Histogram of the durations of the 552 cases scheduled t $\dot{\dot{Q}}$ be a cholecystectomy in the data set．The data are plotted witl｜ a logarithmic axis．A normal distribution curve is superims． posed．The arrow marks the 0.05 percentile of case duration．
wait for the second patient to be ready would be $0.05^{\text {d }}$ Thus，when using the 0.05 percentile，the＂earliest star． time＂of the second case would be 1.7 h after the cholecystectomy was started．

When there are hundreds of previous cases of thè same scheduled procedure，an appropriate interpreta总 tion of the 0.05 percentile is that the risk is 0.05 of 㒴 patient not being ready for surgery when the OR team iథ్ิㅗ available having completed the preceding case in the $\stackrel{\leftrightarrow}{\circ}$ OR．However，in many instances there are only a few （e．g．，two）previous case durations of the same schedule ${ }_{\$}$ procedure available to predict the duration of a future case．${ }^{8,9}$ When there are small numbers of previous cases迢 ＂prediction bounds，＂not percentiles，are relevant． prediction bound for a single future observation is value that will，with a specified degree of confidence，b庆్ర exceeded by the next randomly selected observation $\frac{0}{2}$ from a population．The specified degree of confidence then equals one minus the prediction bound．Thus， 0.05 prediction bound provides a 0.05 risk of the OR staff waiting for the patient．For small numbers of cases？ the value for the 0.05 prediction bound can differ sub stantially from the value of the 0.05 percentile．
A prediction bound incorporates two sources of vari－ ability in an estimate for the duration of a case．First， there is variability intrinsic to the scheduled procedure， as shown in figure 1 ．This source of variability exists whether there are two previous cases＇durations or hun－ dreds of previous cases＇durations．Second，there is vari－ ability in the estimates of the parameters．Because of the small number of previous cases＇durations available to estimate the parameters，the estimated values of the parameters may differ from what they would have been had there been hundreds of previous cases＇durations


Fig．2．Probability distributions for the duration of a future cholecystectomy based on a priori data from two（dotted curve） or 552 （solid curve）previous case durations．Both curves use values for the sample mean and standard deviation of the log－ arithms of case duration obtained using the 552 previous cases． The arrow marks the 0.05 prediction bound for case duration based on there being data from two previous cases．
available．For example，the two curves in figure 2 show the probability distributions for the duration of a future cholecystectomy based on a priori data from two or 552 previous case durations．Both curves use values for the sample mean and standard deviation of the logarithms of case duration that were obtained using the 552 previous cases．Both curves were drawn assuming that the loga－ rithms of case durations follow a normal distribution． The solid curve for 552 previous cases is the same as the one shown in figure 1．The dotted curve，in contrast， gives the probability distribution obtained assuming that the mean and standard deviations were obtained from only two previous cases＇durations．The use of only two previous cases＇durations resulted in greater uncertainty in the accuracy of the duration of the future case．Con－ sequently，the dotted curve in figure 2 is wider than the solid curve．Whereas the 0.05 prediction bound using 552 cases equals the 0.05 percentile or 1.7 h （fig．1），the 0.05 prediction bound using two cases equals 0.3 h （fig．2）．
The focus of this paper was to test different statistical methods to calculate 0.05 prediction bounds for case duration．

## Rationale for Cboosing $\tau=0.05$

We used a value of $\tau=0.05$ in our study based，in part， on the salaries of patients and OR staff．Using recent median annual salaries in the United States，the value $\ddagger$ of $C_{O R} \cong \$ 549,780$ for a surgical team with an anesthesiol－ ogist，a general surgeon，two OR nurses，and a full－time equivalent housekeeper（representing the work of，for example，unit assistants and central sterilization personnel in caring for the patient）．As recommended by the Panel on Cost－effectiveness in Health and Medicine，${ }^{10}$ to value pa－

[^1]tients＇time we used the average wage rate of people older than 16 years in the United States： $\mathrm{C}_{\mathrm{pt}} \cong \$ 27,196 . \ddagger$ Then， $\tau=\$ 27,196 /(\$ 549,780+\$ 27,196) \cong 0.05$ ．

Higher or lower values of $\tau$ may be appropriate be－ cause the valuation of patients＇versus OR staff＇s time varies among hospitals and countries，among other situ－ ations．However，based on the salary argument，we think that setting the risk that the OR suite staff will wait for the patient at $\tau=0.05$ is a reasonable compromise between the value of patients＇and OR staff＇s time．

## Case Duration Data Used in this Study

We tested statistical methods to calculate 0.05 predic tion bounds using case duration data from the Universit嘍 of Iowa．The cases were performed between July $1 \underset{\underset{\circ}{\circ}}{\stackrel{\circ}{~}}$ 1994，and July 1，1997，at the tertiary surgical suite o ambulatory surgery center．＂Case duration＂was define導 as the time from when the patient entered the OR ii which he or she had surgery to the time he or she left thein OR．Entrance and exit times from the OR were recorde $\frac{\stackrel{\omega}{\omega}}{\underline{\omega}}$ by OR nurses when the patients entered and exited fron ${ }^{\frac{2}{0}}$ the OR using clocks that were synchronized throughou践 all ORs in these two surgical suites．Two checks were applied to the times by the OR information system whe蛋． a dedicated data entry clerk entered the data later tha寓 day．First，the entrance and exit times had to concu券 temporally with other recorded times for that case（e．g $g_{\frac{\circ}{\square}}^{\frac{\circ}{⿺}}$ the time of induction of anesthesia）．Second，the calcu䨌 lated case durations were compared automatically to the durations of previously performed cases of the same procedure．Discrepancies were addressed the next working day with the OR nurse or nurses who recorde ${ }_{6}^{\circ}$ the times．
The cases were classified based on their 8，808 different scheduled procedures．If a procedure was schedule $\stackrel{\text { ¢ }}{\mathscr{\Phi}}$ with more than one Current Procedural Terminolog $\stackrel{\rightharpoonup}{\circ}$ （CPT）code，that combination of scheduled codes wå̀ considered to characterize a unique scheduled proce ${ }_{\mathbf{G}}^{\mathbf{\sigma}}$ dure．The observed number of different scheduled pro cedures was reasonable compared with other surgica suites in the United States．${ }^{9}$ We classified each case by it⿳亠丷厂犬 scheduled（ $v s$ s．actual）procedure code because（1）for 嵒 future case for which a prediction bound is being calcu lated，only the scheduled procedure would be known $n_{\text {No }}^{\frac{\circ}{\sim}}$ and（2）for some surgeons and scheduled procedures ${ }^{\wedge}$ the actual procedures occasionally differed from the scheduled procedures．${ }^{11}$

Among the 48,257 cases， 37,699 of the procedures were elective．There were 18,409 series of consecutive elective surgeries in the same OR on the same day with no turnover times exceeding 1 h ．We used these series of consecutive elective cases in part to study the expected number of cases preceding a case in an OR on the day of surgery．
We also used the data to calculate the percentages of cases whose earliest start times can be estimated using
2.5 yr of historical case duration data．This was necessary to determine whether each of the statistical methods to calculate 0.05 prediction bounds would be useful if the method were accurate．We compared the scheduled procedures of the first 2.5 yr of cases to the scheduled procedures for the last 0.5 yr of cases．During the first 2.5 yr ，there were 40,112 cases．Of the 8,145 operations performed in the last $0.5 \mathrm{yr}, 3,717$ were elective cases preceded by another elective case in the same OR on the same day with the turnover time not exceeding 1 h ．The cases performed in these 3,717 patients were compared with the procedures of the 40,112 patients from the first 2.5 yr ．

## Testing Prediction Bounds Assuming that the Logarithms of Case Durations Follow a Normal Distribution（＂Parametric Method＂）

When the natural logarithms of case durations follow a normal distribution，the 0.05 prediction bound equals ${ }^{8,12}$

$$
\begin{equation*}
\exp \left(\overline{\mathrm{T}}+\mathrm{s} \cdot \sqrt{1+1 / \mathrm{N}} \cdot \mathrm{~T}^{-1}[\mathrm{~N}-1,0.05]\right) \tag{1}
\end{equation*}
$$

where $\overline{\mathrm{T}}=$ the mean of the natural logarithms of the N previous case durations，$s=$ the standard deviation of the natural logarithms of the N previous case durations， and $\mathrm{T}^{-1}[\mathrm{~N}-1, \tau]=$ the $\tau$ th percentile of the Student $t$ cumulative distribution function with $(\mathrm{N}-1)$ degrees of freedom．To calculate this parametric prediction bound， case durations must be available from at least two pre－ vious cases of the same scheduled procedure because $\mathrm{N} \geq 2$ is needed to calculate the standard deviation．
For example，we used this equation to calculate the location of the arrows in figures 1 and 2 ．The value of $=\mathrm{T}^{-1}$ $[552-1,0.05]=-1.648$ ．For $N=552, \bar{T}=0.967$ ，and $\mathrm{s}=0.266$ ，the 0.05 prediction bound equaled $\exp (0.967+0.266 \cdot \sqrt{1+1 / 552} \cdot[-1.648])=1.7 \mathrm{~h}$ ． When the 552 case durations were sorted and the 0.05 percentile was found empirically，the value also equaled 1.7 h ．The value of $\mathrm{T}^{-1}[2-1,0.05]=-6.314$ ．For $\mathrm{N}=2$ ， the 0.05 prediction bound equaled $\exp (0.967+$ $0.266 \cdot \sqrt{1+1 / 2} \cdot[-6.314]=0.3 \mathrm{~h}$ ．
This parametric equation for the 0.05 prediction bound assumes that the logarithms of previous cases＇ durations follow a normal distribution．This assumption may not hold sufficiently well for the 0.05 prediction bounds to be accurate．To determine the accuracy of 0.05 parametric prediction bounds，we analyzed the data set in the manner we previously reported．${ }^{8,13}$

## Testing 0．05 Prediction Bounds Calculated Using the Nonparametric Method

We repeated the analysis that we performed for para－ metric 0.05 prediction bounds using nonparametric 0.05 prediction bounds．The nonparametric method has the advantage of not assuming that logarithms of case dura－ tions are normally distributed．These nonparametric
bounds were calculated using the approach described by Beran et al．${ }^{14}$ Provided $\mathrm{N} \geq 19$ ，the 0.05 nonparametric prediction bound equals the $(0.05(\mathrm{~N}+1)-1) /(\mathrm{N}-1)$ percentile of the N numbers．${ }^{14}$

## Testing 0．05 Prediction Bounds Calculated by <br> Having Each Patient Ready for Surgery at a Fixed <br> Number of Hours before the Scheduled End of the <br> Preceding Case in the Operating Room

An economically rational strategy for scheduling elec－ tive cases is to use the mean of the durations of previous cases of the same scheduled procedure to predict tho्ర duration of a future case．${ }^{15}$ A corresponding strategy fo $\stackrel{\underset{ }{3}}{ }$ the problem considered in this study is to subtract $\frac{8}{9}$ specified number of hours from the mean of previou $\overbrace{9}^{7}$ cases＇durations．We studied this strategy because it is 零 method currently used by surgical suites．
We considered the rule whereby patients are asked to arrive sufficiently early to be ready for surgery 1.5 变 before the scheduled end of the preceding case in the OR．If the mean of previous cases of the same schedule $\stackrel{\Phi}{\$}$ procedure type was briefer than 1.5 h ，then the patien would be asked to arrive sufficiently early to be read需 when the preceding case in the OR starts．We used 1.5 置 because we found by trial and error that it gave a risk o ${ }_{6}^{\text {² }}$ the OR staff waiting for the patient of $0.050 \pm 0.00 \stackrel{\text { 雱 }}{ }$ when applied to all cases in the data set．

## Testing the Parametric Method When Applied to More than One Preceding Case in the Same Operating Room

A case may be preceded in its OR by two cases and the్ర turnover time between the two cases．In the data set ${\underset{N}{n}}_{\vec{N}}$ there were 11，444 pairs of consecutive elective cases ii $\stackrel{\text { Q }}{ }$ the same OR on the same day with no turnover time $\stackrel{\text { on }}{0}$ exceeding 1 h and with at least two previous cases of the same scheduled procedure for each of the two cases iiw the series．We evaluated two strategies for predicting the $\frac{8}{8}$ time to complete the pairs of cases．
The actual time to complete a pair of cases and thĕ turnover time between the pair of cases was compared with the sum of the 0.05 prediction bounds for each o the two cases and the turnover time，using the metho ${ }^{\circ}$ of analysis that we reported previously．${ }^{8,13}$ The $0.0{ }^{\circ}$ prediction bound for the turnover time equaled 10 min by both parametric and nonparametric methods．This method needed to be tested in part because we as－ sumed ${ }^{15}$ that the durations of the two cases in each pair were statistically independent．
The 0.05 prediction bound for the time to complete a pair of cases and the turnover time between the pair of cases was also estimated by Monte－Carlo computer sim－ ulation．A duration for each of the two cases in the pair was obtained by making a random draw from its appro－ priate Student $t$ distribution（equation 1）．The process

Table 1．Percentages of Cases Whose Earliest Start Times Can Be Estimated Using 2.5 yr of Historical Case Duration Data

| Number of Previous Cases Used to Predict the Duration of the Preceding Case in the Same Operating Room | Percentages of Cases（Mean $\pm$ Standard Error） |  |
| :---: | :---: | :---: |
|  | Limiting Consideration to Cases that Were Preceded by Another Elective Case $(\mathrm{N}=3,717)$ | Including Cases that Were a＂First－Start＂in an Operating Room（ $\mathrm{N}=8,145$ ） |
| 19 or more | $62.4 \pm 0.8$ | $82.8 \pm 0.4$ |
| 2 or more | $84.5 \pm 0.6$ | $92.6 \pm 0.3$ |
| 1 or more | $88.5 \pm 0.5$ | $94.7 \pm 0.2$ |

was repeated thousands of times，until the $99 \%$ two－ sided confidence interval for the 0.05 quintile for the sum of the durations was less than $5 \mathrm{~min} .{ }^{16}$ Student $t$－distributed random numbers were generated by the T3T＊algorithm．${ }^{17}$
If the time that a patient would be asked to be ready for surgery equals the sum of the three 0.05 prediction bounds，and if the resulting risk of the OR staff waiting for the patient is less than 0.05 ，then the sum of 0.05 prediction bounds would be the earliest time the patient needs to be ready for surgery．On the day of surgery，the patient could call the surgical suite or vice versa to learn how much later than the original estimate he or she should arrive at the surgical suite．We show in the Appendix that the $\tau=0.05$ prediction bound for the duration of a case based on the number of hours（d） because the case started equals

$$
\begin{align*}
& \exp \left(\overline{\mathrm{T}}+\mathrm{s} \sqrt{1+1 / \mathrm{N}} \cdot \mathrm{~T}^{-1}(\mathrm{~N}-1\right. \\
&  \tag{2}\\
& \left.\tau+(1-\tau) \cdot \mathrm{T}\left(\mathrm{~N}-1, \frac{\ln (\mathrm{~d})-\overline{\mathrm{T}}}{\mathrm{~s} \sqrt{1+1 / \mathrm{N}}}\right)\right)
\end{align*}
$$

We tested this method for cases in the data set with durations that were at least $\mathrm{d}=0.5,1.0$ ，or 1.5 h long．

## Results

## Characteristics of Surgical Cases

The mean $\pm$ SD of the number of cases in each series of elective cases in an OR was $2.0 \pm 1.1$ cases，with an SEM of 0.01 cases．Among the elective cases， $87 \pm 0.2 \%$ were preceded by zero or one case．
To calculate a 0.05 percentile empirically necessitates that there be at least 19 previous case durations because

[^2]$0.05=1 /(19+1)$ ．Table 1 ，row 1 ，shows that with 2.5 yr of historical data， 19 or more previous cases of the same scheduled procedure type would be available to calcu late a 0.05 percentile for $62 \pm 1 \%$ of elective case preceded by another elective case in the same OR on the $\stackrel{\stackrel{\rightharpoonup}{3}}{3}$ same day．
Table 1，row 2，shows that，with 2.5 yr of data，clerk could use parametric methods to determine when patient should be ready for surgery for $84 \pm 1 \%$ of cases precede ${ }^{\circ}$ by another case in the same OR on the same day．$\delta$

## Calculation of Prediction Bounds for the Duration of the Preceding Case in the Operating Room

Table 2 shows the percentage of cases for which the OR staff would have to wait for the patient．
The first column shows the results when the paramet ${ }^{\frac{2}{0}}$ ric method was used．The 0.05 prediction bound혼 achieved an actual risk of $0.053 \pm 0.001$ for the OR staf葿 to wait for the patient．If the minimum number of pre vious cases used to calculate the parametric predictiof bounds was 19 instead of 2 ，then the achieved risk wa $\stackrel{\rightharpoonup}{3}$ more accurate at $0.050 \pm 0.001$ ．
The second column shows results for the nonparamet ric method．It performed no better than the parametri凶 method．
In the third column we provide results from when w $\underset{8}{8}$ estimated the 0.05 prediction bound by having eaclo̊ patient ready for surgery 1.5 h before the scheduled en黑 of the preceding case in the OR．By design，the overal居 risk of the OR staff waiting for the patient equale ${ }^{\Phi}$ $0.050 \pm 0.001$ ．Increasing the minimum number of pre ${ }_{\sim}^{\circ}$ vious cases from at least two to at least 19 caused the risle to change from $0.050 \pm 0.001$ to $0.035 \pm 0.001$ ．Thi휼 was because of the marked dependence of the risk of th甾 OR staff waiting for the patient on the mean of previous cases＇durations．When the mean of previous cases＇du－ rations was less than or equal to 1.5 h ，the patient was （by definition）always available when the preceding case in the OR was completed．The risk of the OR staff waiting for the patient always equaled 0.000 ．When the mean of previous cases＇durations was longer than 3.5 h ， the risk was $0.143 \pm 0.004$ for two or more previous cases and $0.100 \pm 0.004$ for 19 or more previous cases．The improvement in the accuracy of the prediction bounds for the longer case durations，which was achieved by increas－

Table 2．Comparison of Statistical Methods＇Abilities to Predict the Correct Answer（5\％）that the Risk Was 0.05 that Case Duration Would Be Briefer than Expected

| Number of Previous Cases | Mean Case Duration（h） | Parametric Method＊ | Nonparametric Method＊ | Mean Minus $1.5 \mathrm{~h}^{*}$ | Sample Size |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 or more | All |  |  | $5.4 \pm 0.1$ | 38，454 |
|  | $\leq 1.5$ |  |  | $0.0 \pm 0.0$ | 6，716 |
|  | 1．5－3．5 |  |  | $2.4 \pm 0.1$ | 21，726 |
|  | $>3.5$ |  |  | $15.6 \pm 0.4$ | 10，012 |
| 2 or more | All | $5.3 \pm 0.1$ |  | $5.0 \pm 0.1$ | 35，625 |
|  | $\leq 1.5$ | $4.8 \pm 0.3$ |  | $0.0 \pm 0.0$ | 6，155 |
|  | 1．5－3．5 | $5.2 \pm 0.2$ |  | $2.4 \pm 0.1$ | 20，338 |
|  | $>3.5$ | $5.7 \pm 0.2$ |  | $14.3 \pm 0.4$ | 9，132 |
| 19 or more | All | $5.0 \pm 0.1$ | $5.1 \pm 0.2$ | $3.5 \pm 0.1$ | 21，755 |
|  | $\leq 1.5$ | $5.0 \pm 0.3$ | $4.4 \pm 0.3$ | $0.0 \pm 0.0$ | 4，132 |
|  | 1．5－3．5 | $5.1 \pm 0.2$ | $5.5 \pm 0.2$ | $2.2 \pm 0.1$ | 12，718 号 |
|  | $>3.5$ | $4.9 \pm 0.3$ | $4.7 \pm 0.2$ | $10.0 \pm 0.4$ | 4，905 |

＊Percentage of cases（ $\pm$ standard error）that would be delayed using the different methods of predicting the earliest starting time．
ing the number of previous cases，had the effect of wors－ ening the overall accuracy of the method．

## Application of the Parametric Method to More than One Preceding Case in the Same Operating Room

If the patient having surgery after two preceding cases and a turnover was ready for surgery at the time corre－ sponding to the sum of the three 0.05 prediction bounds，the risk of the OR staff waiting for the patient would be $0.016 \pm 0.001$ ．If computer simulation were used，the risk of the OR staff waiting would be $0.059 \pm$ 0.001 ．

If the patient contacts the surgical suite on the day of surgery，the 0.05 prediction bound for the duration of the first of two preceding cases could be adjusted based on the number of hours since the case started．If this preceding case in the OR had been underway for 0.5 ， 1.0 ，or 1.5 h ，then the 0.05 prediction bounds achieved actual risks for the OR staff to wait for the patient of $0.055 \pm 0.001,0.058 \pm 0.001$ ，and $0.056 \pm 0.001$ ， respectively．

## Discussion

## Implications of Findings

Weiss showed previously that，based on a surgical suite＇s relative valuation ${ }^{1}$ of patients＇waiting time to staff＇s idle time，there is an optimal number of hours before the scheduled end of the preceding case in a patient＇s OR that the patient should be ready for sur－ gery．${ }^{4}$ We used actual case duration data to test statistical methods to estimate the earliest start time of a case so that Weiss＇theory can be programmed into surgical services information systems．

The parametric method to calculate prediction bounds assumes that the logarithms of case durations follow a normal distribution．Although this assumption may not be strictly satisfied，figure 1 suggested that for cholecys－ tectomies the logarithms of previous cases＇durations
can follow a distribution that is close to being normall distributed．Case durations have been found to be $\log _{\frac{1}{2}}^{\underline{p}}$ normally distributed，${ }^{18}$ and statistical methods that ass sume case durations follow log－normal distributions have been used successfully in applications．${ }^{8,13}$ Therefore，we suspected that the parametric equation for the 0.0 零 prediction bound would perform sufficiently well for the⿳⺈⿵冂𠃍冖⺝刂 risk that the OR staff would wait for the patient to b商 approximately 0.05 if the patient were ready for surger at the time specified by the 0.05 prediction bound．W $\frac{\circ}{\circ}$ found that 0.05 prediction bounds calculated using the parametric method achieved actual risks of 0.053 0.001 for the OR staff to wait for the patient，which we consider to be very accurate．
We found that the parametric method was preferableî응 to having patients ready for surgery a fixed number o $\stackrel{8}{6}$ hours before the scheduled end of the preceding case int the OR．First，when the latter method was used，increas ing the minimum number of preceding cases from $a \overrightarrow{8}$ least two to at least 19 caused the risk to change from $0.050 \pm 0.001$ to $0.035 \pm 0.001$ ．In contrast，the paramet ric method became more accurate．Second，there was 密 large dependence of the risk of the OR staff waiting for the్ర patient on the mean of previous cases＇durations．

## Updating the Earliest Start Time for Series of Successive Cases

Among surgical suites in the United States，there wa§ an average of 2.0 cases per OR each work day．${ }^{19}$ In our data set，the mean number of cases in each series of elective cases in an OR was also 2.0 cases． $87 \%$ of patients had zero or one preceding case in their OR．
Some surgical suites have scheduled delays between series of cases（e．g．，a morning and afternoon session separated by lunch）．When there is a scheduled delay， the cases after the delay start as if there were no preced－ ing cases in the OR．The use of scheduled delays in surgical suites increases the applicability of statistical methods for zero or one preceding cases．

Nevertheless，a method is needed to choose the times at which the patients with two or more preceding cases should be ready for surgery．We showed that when there are a series of successive cases in an OR，the sum of 0.05 prediction bounds can be used before the day of surgery as the earliest time the patient needs to be ready forsur－ gery．｜｜This approach is conservative from the patient＇s perspective，in that the risk of the OR staff waiting for the patient is less than 0.05 ．
An alternative approach is for the 0.05 prediction bound for a series of cases to be calculated by using Monte－Carlo computer simulation．However，for many cases，there are only a few previous cases of the same scheduled procedure type（table 1）．${ }^{9}$ With a small num－ ber of cases，the Student $t$ densities had long lower tails （fig．2）．It is the lower tail that is used for calculating 0.05 prediction bounds．Due to the long lower tails，hundreds of thousands of Student $t$－distributed random numbers had to be generated for the precision of the estimate to be within 5 min ．Thus，although this method yielded accurate results，the computational effort was substantial compared with the use of equation 1 ，which may make this approach less practical．
On the day of surgery，the patient can call the surgical suite or vice versa so that the patient can get an updated time to arrive at the surgical suite based on the updated earliest start time of the first of two preceding cases in the patient＇s OR．We found that the parametric method can accurately predict the 0.05 prediction bound for the time remaining in a case．If this method is used，patients may then have shorter waits while maintaining the risk that OR staff will be idle at less than 0.05 ．Our experi－ ence is that this concept is readily understandable by hospital staff and patients．Updating a patient＇s arrival time may be helpful if the second of two preceding cases has not started when the patient calls．Having the patient call may also be particularly useful if the number of previous cases＇durations available to estimate the pa－ rameters for the prediction bound for the first of the two preceding cases is small，and as such，the 0.05 prediction bound is very brief，as in figure 2.
Updating the start time provides flexibility to the sur－ gical suite in moving cases from one OR to another while maintaining a relative valuation of patients＇waiting time to staff idle time of 0.05 ．We found that updating the start time can be straightforward for patients who live close to the surgical suite，are staying at hotels near the hospital，or are coming to the surgical suite from a ward or intensive care unit．

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## Time that Patients Should Arrive at the Surgical Suite versus the Time that They Should Be Ready for Surgery

We focused on predicting the time when a patient needs to be ready for surgery．Based on the estimated earliest start time of a patient＇s case，a clerk will need to decide when the patient should arrive at the surgical suite．The difference between the estimated earliest start time and the time at which the patient should be asked to arrive varies among surgical suites because of differ－ ences in average patient punctuality，time necessary to change into a hospital gown，availability of medications ${ }_{\text {o }}$ and turnover times，among other factors．For long pree ceding cases in the patient＇s OR，variability in thes適 factors is relatively unimportant compared with the vario ability in the duration of the preceding case．${ }^{3}$ For brie胥 preceding cases，variability in these factors may be in portant．

## Cancellation on the Day of Surgery of a Preceding Case

The theory developed to balance the cost of a patien waiting on the day of surgery versus the cost of OR staf waiting for the patient assumes that the preceding cas蝈． is performed．${ }^{4}$ Institutions with a high percentage o 0 cancellations can incorporate the risk of cancellatio into its decision－making regarding when patients shoul $\frac{\overline{4}}{\frac{6}{4}}$ be ready for surgery．For example，if the proportion o 0 appropriately scheduled cases that cancel on the day or surgery equals 0.03 ，then a 0.02 prediction bound woul $\overrightarrow{\text { क् }}$ be used instead of a 0.05 prediction bound to maintaii the risk of the OR staff waiting for the patient at 0.05 ．瞦 an OR has a cancellation rate greater than 0.05 ，the 18 even if every patient scheduled for elective surgery whot shows up were to be ready for surgery at the start of the workday，the risk of the OR staff waiting for a patien would always exceed 0.05 ．

## Other Applications of Predicting Earliest Start Times of Cases

We found that there are other ways that 0.05 predic⿳⺈⿴囗十大冖ํ tion bounds for preceding cases in ORs can be used First，family members and friends of patients in the hospital need to decide when to come to the hospital or군 the day of surgery．Second，the equation for the $0.0 \%$ prediction bound of the time remaining in a case（equa－ tion 2）can be used for family members wanting to know the earliest time a case is likely to end so that they can take a walk or perform other tasks．Third，shortening the preoperative fasting period to a few hours ${ }^{20,21}$ can be difficult to manage in practice for patients who are not the first cases of the day because of uncertainty in know－ ing the earliest time at which their cases will start．
We reviewed the theory for determining when a pa－ tient should be ready for surgery．We showed that the 0.05 prediction bound for a case can be estimated accu－
rately assuming that the logarithms of case durations follow a normal distribution.

## References

1. Dexter F: Design of appointment systems for preanesthesia evaluation clinics to minimize patient waiting times: A review of computer simulation and patient survey studies. Anesth Analg 1999; 89:925-31
2. Pollard JB, Zboray AL, Mazze RI: Economic benefits attributed to opening a preoperative evaluation clinic for outpatients. Anesth Analg 1996; 83:407-10
3. Rotondi AJ, Brindis C, Cantees KK, DeRiso BM, Ilkin HM, Palmer JS, Gunnerson HB, Watkins WD: Benchmarking the perioperative process. I. Patient routing systems: A method for continual improvement of patient flow and resource utilization. J Clin Anesth 1997; 9:159-67
4. Weiss EN: Models for determining estimated start times and case orderings in hospital operating rooms. IIE Transactions 1990; 22:143-50
5. Richins S, Holmes M: Waiting for satisfaction. J Healthcare Manag 1998;43: 281-5
6. Otte DI: Patients' perspectives and experiences of day case surgery. J Adv Nurs 1996; 23:1228-37
7. Huang XM: Patient attitude towards waiting in an outpatient clinic and its applications. Health Serv Manag Res 1994; 7:2-8
8. Zhou J, Dexter F: Method to assist in the scheduling of add-on surgical cases-upper prediction bounds for surgical case durations based on the log normal distribution. Anesthesiology 1998; 89:1228-32
9. Dexter F, Macario A: What is the relative frequency of uncommon ambulatory surgery procedures in the United States with an anesthesia provider? Anesth Analg 2000; 90:1343-7
10. Weinstein MC, Siegel JE, Gold MR, Kamlet MS, Russell LB: Recommendations of the panel on cost-effectiveness in health and medicine. JAMA 1996; 276:1253-8
11. Dexter F: Application of prediction levels to operating room scheduling. AORN J 1996; 63:607-15
12. Dahiya RC, Guttman I: Shortest confidence and prediction intervals for the log-normal. Can J Stat 1982; 10:277-91
13. Dexter F, Macario A, O'Neill L: A strategy for deciding operating room assignments for second-shift anesthetists. Anesth Analg 1999; 89:920-4
14. Beran R, Hall P, Hall PG: Interpolated nonparametric prediction intervals and confidence intervals. J Roy Statist Soc Ser B 1993; 55:643-52
15. Dexter F, Traub RD, Qian F: Comparison of statistical methods to predict the time to complete a series of surgical cases. J Clin Monit Comput 1999; 5:45-51
16. Klugman SA, Panjer HH, Wilmot GE: Loss Models. From Data to Decisions. New York, John Wiley \& Sons, Inc., 1998, p 327
17. Fishman GS: Monte Carlo Concepts, Algorithms, and Applications. New York, Springer-Verlag, 1999, pp 207-9
18. Strum DP, May JH, Vargas LG: Modeling the uncertainty of surgical procedure times: Comparison of the log-normal and normal models. Anesthesiology 2000; 92:1160-7
19. Solovy A: Benchmarking guide 99. Hosp Health Network 1999; 73:49-62
20. Warner MA, Caplan RA, Epstein BS, Gibbs CP, Keller CE, Leak JA, Maltby R, Nickinovich DG, Schreiner MS, Weinlander CM: Practice guidelines for preoperative fasting and the use of pharmacologic agents to reduce the risk o $\Phi$ pulmonary aspiration. Application to healthy patients undergoing elective pross cedures. Anesthesiology 1999; 90:896-905
21. Ferrari LR, Rooney FM, Rockoff MA: Preoperative fasting practices i pediatrics. Anesthesiology 1999; 90:978-80

## Appendix

To derive equation 2 , the $\tau$ th prediction bound $\mathrm{b}=\exp \left(\overline{\mathrm{T}}+\mathrm{s} \frac{\frac{\infty}{\bar{\omega}}}{\frac{\Phi}{2}}\right.$ $\sqrt{1+1 / \mathrm{N}} \cdot \mathrm{T}^{-1}[\mathrm{~N}-1, \tau]$, where $\mathrm{T}^{-1}[\mathrm{~N}-1, \tau]$ represents the $\tau$ 傐. percentile of the Student $t$ cumulative distribution function witloi ( $\mathrm{N}-1$ ) degrees of freedom. ${ }^{8,12}$ Rearranging terms, $\tau=\mathrm{T}(\mathrm{N}-1 \stackrel{3}{3}$ $[\ln (\mathrm{b})-\overline{\mathrm{T}}] /[\mathrm{s} \sqrt{1+1 / \mathrm{N}}])$. Because $\mathrm{b}>\mathrm{d}$, the number of hours sinc ${ }_{6}$ the case started is $\tau=(\mathrm{T}(\mathrm{N}-1,[\ln (\mathrm{~b})-\overline{\mathrm{T}}] /[\mathrm{s} \sqrt{1+1 / \mathrm{N}]})-\mathrm{T}(\mathrm{N} \stackrel{-}{\stackrel{\rightharpoonup}{\mathrm{W}}}$ 1, $[\ln (\mathrm{d})-\overline{\mathrm{T}}] /[\mathrm{s} \sqrt{1+1 / \mathrm{N}}])) /\left(1-\mathrm{T}\left(\mathrm{N}-1,[\ln (\mathrm{~d})-\overline{\mathrm{T}}] /\left[\mathrm{s} \sqrt{ } 1+1 \frac{\mathrm{C}}{6}\right.\right.\right.$ $\mathrm{N}])$ ). Solving this equation for b gives equation 2.


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[^1]:    $\ddagger$ Sites accessed June 12，1999：http：／／www．pohly．com／salary＿anes．shtml， http：／／www．aana．com／library／costeffect．asp，http：／／www．pohly．com／salary＿gene． shtml，http：／／www．nurseweek．com／features／97－12／earnsrvy．html，ftp：／／ftp．bls．gov／ pub／special．requests／lf／aat39．txt，and ftp：／／ftp．bls．gov／pub／special．requests／ lf／aat39．txt

[^2]:    § Adding to this percentage the cases that were＂first－starts＂in an OR，para－ metric methods could be used to determine when $93 \pm 0.3 \%$ of patients should be ready for surgery（table 1，row 2 ，column 2 ）．This $93 \%$ value can be increased further．We consider an OR with two scheduled cases．The first case has one or zero previous case durations of the same scheduled procedure（s）．The second case has many previous cases of the same scheduled procedure（s）．The sequence of cases can be switched so that the case with historical case duration data is performed first．Specifically，cases were switched if（1）a case was followed in the same OR on the day of surgery by another elective case；（2）the first of the two cases was of a scheduled procedure that in 2.5 yr no more than one case of the same scheduled procedure had been performed；（3）the case that followed the case was of a scheduled procedure with two or more previous cases of the same scheduled procedure type；and（4）the case that followed was itself not followed by another case．Making such switches increased the percentage of cases for which the parametric method could be used to $95 \pm 0.2 \%$ ．

[^3]:    ｜｜Alternatively，the durations of previous＂common＂pairs of cases could，in theory，be used directly in the analytical expression for the 0.05 prediction bound．However，there were few＂common＂pairs of cases．Among the 3，717 pairs of cases with a turnover time in the $0.5-\mathrm{yr}$ data set，only $26 \pm 1 \%$ of the pairs had two or more like pairs in the earlier 2.5 yr of data．

