# Population Pharmacokinetics and Pharmacodynamics of Thiopental: The Effect of Age Revisited 

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#### Abstract

The authors have previously attributed the mechanism for the $\mathbf{5 0 - 6 7 \%}$ decrease in the required dose of thiopental for induction of anesthesia in aged human patients to a decrease in the initial distribution volume for thiopental. Using a larger group of patients and volunteers studied in the laboratory, the authors have re-examined thiopental pharmacokinetics and EEG pharmacodynamics relative to age. A population data analysis approach (NONMEM), using a three-compartment model, was used to analyze bolus and rapid iv infusion thiopental serum concentration versus time data from 64 subjects. A one-compartment model was also used on the first $\mathbf{1 0} \mathbf{~ m i n}$ of serum concentration data to focus only on the initial distribution phase. The population pharmacokinetic analysis demonstrated that when thiopental is administered via an iv bolus injection, traditional pharmacokinetic models limit the accurate characterization of thiopental distribution phenomena. Using the rapid iv infusion data, the pharmacokinetic mechanism for the decreased thiopental dose requirement in the elderly was a decreased rapid intercompartment clearance. Thiopental distribution from the central compartment of the three-compartment model to the rapidly equilibrating compartment (rapid intercompartment clearance) decreased $27 \%$ between the ages of $35-80 \mathrm{yr}$ and decreased $34 \%$ in the one-compartment analysis. EEG spectral edge versus time data from 37 subjects was analyzed with a semiparametric modelling approach to remove the disequilibrium between thiopental serum concentration and the spectral edge. A population data analysis (NONMEM) was performed with several pharmacodynamic models. There was no age-related change in brain responsiveness or pharmacodynamics when the spectral edge is used as a measure of drug effect. (Key words: Age factors. Anesthetics, intravenous: thiopental. Brain: electroencephalography. Modelling, population analysis. Pharmacodynamics: thiopental. Pharmacokinetics: thiopental.)


WE PREVIOUSLY reported that anesthetic requirements for thiopental in humans decreased $50-67 \%$ over the age range of $20-80 \mathrm{yr}$ using the EEG as a measure of CNS drug effect. ${ }^{1}$ In our previous publication we used a tra-

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[^0]ditional two-stage data analysis approach to examine the effects of increasing age on thiopental pharmacokinetics and pharmacodynamics. This approach required a complete thiopental serum concentration or EEG effect versus time curve for each subject. These data were then fit to a three-compartment pharmacokinetic model or a pharmacodynamic effect model using nonlinear least-squares regression. Each subject generated pharmacokinetic or pharmacodynamic parameters (first stage). The effect of age on these parameters were analyzed with linear regression (second stage). The initial distribution volume of thiopental decreased from $20-251$ in the $20-\mathrm{yr}$-old subjects to 3-7 l in the elderly. Pharmacodynamic modelling of the thiopental EEG spectral edge changes could not demonstrate an age-related change in brain responsiveness.

We have recently re-examined thiopental pharmacokinetics and pharmacodynamics relative to age for several reasons: 1) other investigators studying thiopental pharmacokinetics have described an age-related distribution phase pharmacokinetic mechanism that is different from what we reported; ${ }^{2}$ 2) newer pharmacokinetic and pharmacodynamic data analysis techniques to examine this issue are now available; ${ }^{3-7} 3$ ) additional data on the pharmacokinetics and pharmacodynamics of thiopental have been generated in our laboratory. ${ }^{8}$

Using a population pharmacokinetic and pharmacodynamic analysis (NONMEM), we examined the following issues: 1) is there a difference in distribution phase pharmacokinetics between iv bolus and rapid iv infusion administration of thiopental? In our previous analysis ${ }^{1}$ both methods of thiopental administration were used to generate pharmacokinetic data; 2) does age and weight affect thiopental distribution pharmacokinetics? 3) does age affect thiopental EEG pharmacodynamics?

## Methods

## Pharmacokinetic Patient Data

Thiopental serum concentration versus time data from 64 subjects reported by our laboratory over the past 8 yr were used in the pharmacokinetic analysis (table 1). One group included 26 surgical patients previously reported by Homer and Stanski. ${ }^{1}$ These subjects received either an iv bolus ( 15 s ) or rapid iv infusion of thiopental (75$100 \mathrm{mg} / \mathrm{min}$ ) to a defined endpoint of $1-3 \mathrm{~s}$ of isoelectric EEG. An additional 13 patients originally reported in the
pharmacodynamic section of the Homer and Stanski ${ }^{1}$ publication were also included. These patients received a thiopental infusion ( $75-100 \mathrm{mg} / \mathrm{min}$ ) to a defined EEG endpoint, but had arterial serum concentrations measured for only $1 / 4$ to $1 / 2 \mathrm{~h}$. This short duration of blood sampling precluded pharmacokinetic analysis with conventional techniques but can be used in the NONMEM approach.

A group of 20 volunteers and patients from the study reported by Swerdlow et al. ${ }^{8}$ on the effects of "heavy" alcohol intake on thiopental pharmacokinetics and pharmacodynamics was also used in this analysis. Eleven "heavy" drinkers received a thiopental infusion of 100 $\mathrm{mg} / \mathrm{min}$ to a defined EEG endpoint. Five of these heavy drinkers participated in a second study approximately 1 month later. The second pharmacokinetic study data was also included in the analysis. Swerdlow et al. ${ }^{8}$ also studied a control group of six volunteers and three patients who were "social" drinkers. Using a traditional two-stage data analysis approach, Swerdlow et al. determined that thiopental pharmacokinetics were not different between heavy drinkers and control subjects. ${ }^{8}$

To complete the data set for the current study, five elderly surgical patients received a iv bolus of thiopental ( $4 \mathrm{mg} / \mathrm{kg}$ ) with serum sampling for $24-33 \mathrm{~h}$. These subjects were studied by the present authors and have not been reported previously.

The pharmacokinetic data set thus involved 64 subjects, 16 receiving an iv bolus and 48 a rapid iv infusion. The iv bolus was given manually with a syringe over 15 s while a calibrated infusion pump was used for the infusion studies $(75-100 \mathrm{mg} / \mathrm{min})$. For the iv bolus studies, arterial blood was sampled at $1,2,3,5,10,15,30$, and 45 min , then at increasing time intervals to characterize the thiopental elimination phase. For the infusion studies, arterial blood was sampled at $1 / 2-1 \mathrm{~min}$ intervals during the in-
fusion, then at 1-3 min intervals for the next 20 min . For those subjects in whom elimination-phase pharmacokinetics were characterized, subsequent venous sampling occurred at appropriate intervals for 24-52 h.

For any surgical patient receiving a thiopental infusion, general anesthesia was induced $20-30 \mathrm{~min}$ after the initial thiopental administration. Surgical anesthesia was provided by $1-2 \mathrm{mg} / \mathrm{kg}$ of methohexital and $1 \mathrm{mg} / \mathrm{kg}$ of succinylcholine, followed by intubation of the trachea and $1-2 \%$ inspired enflurane with $70 \%$ nitrous oxide. For surgical patients receiving an iv bolus, tracheal intubation and enflurane anesthesia began 3-5 min after the initial iv bolus administration of thiopental. Heavy drinkers and volunteer controls did not receive a general anesthetic. The age range of the 64 subjects in the pharmacokinetic analysis was $23-88 \mathrm{yr}$ and the weight range was $52-118$ kg . Four subjects were female. Twenty-three subjects were $20-40 \mathrm{yr}, 9$ subjects $41-60 \mathrm{yr}$, and 33 subjects $61+\mathrm{yr}$. All patients and volunteers were ASA physical status 1 or 2 without hepatic, respiratory, cardiovascular, or renal disease. Routine laboratory tests were normal in all subjects except one heavy drinker who had abnormal hepatic function tests. Protocols were approved by the Stanford Institutional Review Board and informed consent was obtained from all subjects.

Total (free and protein-bound) serum thiopental concentrations were measured using a high performance liquid chromatographic assay sensitive to $100 \mathrm{ng} / \mathrm{ml} .{ }^{9}$ The same assay was used for all of the above studies.

## Pharmacodynamic Patient Data

Arterial thiopental serum concentration versus spectral edge data from 38 subjects in two previously reported studies were used. ${ }^{1,8}$ Data from 18 of the surgical patients

Table 1. Subject Description and Source for Thiopental Population Pharmacokinetics
$\left.\begin{array}{c|c|c|c|c}\hline \hline & & & \begin{array}{c}\text { Duration of } \\ \text { Sampling } \\ \text { (h) }\end{array} \\ \hline \text { Patients of }\end{array}\right]$

[^1]reported by Homer and Stanski were reanalyzed. Twenty subjects involved in the study of Swerdlow et al. on thiopental pharmacokinetics and pharmacodynamics in heavy drinkers were included in the pharmacodynamic reanalysis. Five of the 11 heavy drinkers were studied on two occasions to generate 16 data sets while the nine control subjects increased the group size to 25 data sets. In Swerdlow's original data analysis, a parametric pharmacodynamic analysis using a traditional two-stage approach of characterizing the thiopental serum concentration versus spectral edge was used. ${ }^{8,10,11}$ The heavy drinkers did not have different pharmacodynamics compared with those from the control subjects. The same EEG recording equipment and waveform analysis software were used in all subjects. The age range of the pharmacodynamic subjects was 24-88 yr and the weight range was $52-118 \mathrm{~kg}$; 20 subjects were $20-40 \mathrm{yr}, 5$ subjects were $41-60 \mathrm{yr}$, and 13 subjects were $61+\mathrm{yr}$.

## Population Pharmacokinetic Data Analysis

The NONMEM nonlinear regression program $\ddagger \S$ was used to derive average population pharmacokinetic parameters for thiopental and to model the influence of the following: age, bodyweight, mode of administration of the drug (bolus vs. infusion), and alcohol intake. The procedure was similar to that performed in our previous study regarding alfentanil. ${ }^{3}$ A modified stepwise approach analogous to multiple stepwise linear regression was used to determine which parameters should be included in a "final," optimal model that has the best fit (lowest -2 log likelihood). To determine which factor would influence the pharmacokinetic parameters, we compared the results obtained when the factor in question was incorporated in the model and (using a value that was freely estimated by the regression program) with the results obtained when the factor was constrained to a fixed value (usually 0 or 1 , depending on the model) corresponding to the null hypothesis, i.e., no effect of the factor of interest. To examine the influence of an individual factor on the model fit, the following criteria were considered: the difference in $-2 \log$ likelihood (asymptotically chi-square distributed), the standard errors of the parameter estimates, the plots of the residuals, and the change in the remaining variability between patients. A conservative $P$ value ( $P$ $<0.005$ ) corresponding to a log likelihood difference of 7.8 was chosen as the limit beyond which a parameter should be included in the final model. This conservative $P$ value was chosen because of the asymptotic nature of the chi-square test.

[^2]The data indicated in table 1, which include distribution and elimination phases, was fit to a three-compartment model with elimination from the central compartment using the same parameters as previously used for alfentanil. ${ }^{3}$ The three-compartment model was statistically preferred over a two-compartment model. Effects of age, body weight, chronic alcohol intake, and the mode of administration (bolus vs. infusion) on the pharmacokinetic parameters were examined.

To focus the pharmacokinetic analysis on the period of maximal relevance for the clinical effect, a separate analysis was performed on the serum concentration data gathered between $1-10 \mathrm{~min}$ after the iv bolus and the serum concentration data during the $3-12-\mathrm{min}$ period of thiopental infusion. The bolus and infusion data was fit to a one-compartment modelll with two parameters: Vd, the volume of distribution that approximates the initial distribution volume of the three-compartment model; and $\mathrm{K}_{\mathrm{e}}$, the rate constant for drug removal, which describes distribution and elimination processes.

## Population Pharmacodynamic Data Analysis

In all of the pharmacodynamic experiments, thiopental was rapidly infused to a defined endpoint evident in the EEG. Using the spectral edge as a measure of effect on the EEG, a time lag (or disequilibrium) was always observed between the measured thiopental serum concentration and the spectral edge value. Furthermore, the effect corresponding to a particular serum concentration of drug during infusion is lower than the effect corresponding to the same serum concentration after the infusion is terminated. A plot of serum concentration versus effect thus exhibits a hysteresis loop, indicating that the site of action of the drug is different from serum. ${ }^{10}$ Sheiner et al. formalized the concept of an effect "compartment" that can be used to incorporate these observations in a "parametric" pharmacodynamic model. ${ }^{11}$ In this approach, the serum concentration versus time data is first fit to a pharmacokinetic model. The effect versus time data is then characterized by simultaneously fitting the data to an effect compartment that estimates the degree of disequilibrium with a first order rate constant $\left(\mathrm{K}_{\mathrm{e} 0}\right)$ and a pharmacodynamic model that relates effect site concentrations to measured effect. This approach has been used previously to describe thiopental pharmacodynamics. ${ }^{1,8,10}$

Recently a "semiparametric" approach to estimating the degree of disequilibrium in drug concentration versus time and effect versus time data has been described. ${ }^{5-7}$ The conceptual approach of this technique is described

T Ebling WF, Arden JR, Holley FO, Scott JC, Stanski DR. A model of anesthetic dose requirement: Pharmacokinetic and pharmacodynamic requirements (abstract). ANESTHESIOLOGY 65:A547, 1986
in figure 1. This approach estimates $\mathrm{K}_{\mathrm{e} 0}$ and calculates the apparent effect-site concentration for each measured effect point without using the assumptions of a pharmacokinetic or pharmacodynamic model, hence the term "semiparametric." The apparent thiopental concentration at the effect site is equivalent to the steady-state thiopental

## NON-PARAMETRIC PD MODEL



Adjust $k_{\text {eo }}$ until hysteresis loop collapses.


Fig. 1. Fundamental basis of semiparametric pharmacodynamic analysis. Following drug administration, the pharmacokinetic processes determine the time course of plasma drug concentration (solid line, left panel). The effect site is linked to the plasma with a first order rate constant, $\mathrm{K}_{\mathrm{e} 0}$. The resulting effect site concentration is translated into pharmacologic effect. The theoretical time course of effect site concentrations is estimated by convolving the plasma concentration with $\mathrm{K}_{\mathrm{c} 0}$ (left panels). If $\mathrm{K}_{\mathrm{e} 0}$ is chosen too large the theoretical concentration ( TCe , dashed line) are left-phase shifted from the actual effect site concentrations ( Ce , symbols). In this example, plotting the TCe as Ce against effect (E) produces a counterclockwise hysteresis loop (top right panel). Choosing $\mathrm{K}_{\mathrm{e} 0}$ too small results in a clockwise hysteresis loop. When $K_{e 0}$ is chosen correctly the hysteresis loop uniquely collapses and the apparent concentration effect relationship is defined. The iterative algorithm varies $\mathrm{K}_{\mathrm{e} 0}$, reducing the area inscribed by the hysteresis. (Reproduced with permission from lecture notes of Lewis B. Sheiner, M.D.)


Fig. 2. The individual thiopental serum concentrations (log scale) versus time curves for 16 subjects who received a rapid iv bolus of thiopental. Concentrations were normalized to a thiopental bolus dose of 400 mg .
serum concentration that would result in the measured effect. For each subject, the thiopental serum concentration and spectral edge was used with the semiparametric modelling approach described above to remove the disequilibrium. The spectral edge versus apparent thiopental effect site concentration data was then fit to $\mathrm{E}_{\text {max }}$ and sigmoid $\mathrm{E}_{\text {max }}$ pharmacodynamic models for all of the data collectively using NONMEM. After choosing the appropriate pharmacodynamic model, the effect of age on the pharmacodynamic parameters was explored.

## Results

Figure 2 displays the individual serum concentration versus time data during the first 10 min for all subjects who received an iv bolus injection of thiopental. Variability in the serum concentrations is greatest in the first minute and progressively decreases until the third minute. After 3 min , the serum concentration decay is relatively consistent and uniform in all subjects. Figure 3 indicates the individual thiopental serum concentration versus time curves for all subjects less than 60 yr during the infusion. Figure 4 indicates the same data for all subjects greater than 60 yr . In both figures 3 and 4, the thiopental infusion was terminated when the EEG in each subject was isoelectric for 1-3 s. Subjects less than 60 yr received more drug compared with subjects greater than 60 yr , reflecting the decreased dose requirement of elderly surgical patients.

## Population Pharmacorinetic Analysis

Table 2A indicates the findings of the stepwise NONMEM regression performed on the bolus and infusion data using the three-compartment pharmacokinetic model. The analysis began with a three-compartment, six-


Fig. 3. The individual thiopental serum concentration (linear scale) versus time curves in 30 subjects less than 60 yr during a thiopental infusion normalized to a rate of $100 \mathrm{mg} / \mathrm{min}$. Five subjects have two separate studies displayed.
parameter pharmacokinetic model with no additional factors present. Next, the initial distribution volume ( $\mathrm{V}_{1}$ ) and metabolic clearance (CL) were both found to be proportional to body weight. Finally, the rate constant $\mathrm{K}_{12}$, which characterizes the initial distribution to the rapidly equilibrating compartment, decreased with age in a linear fashion beginning at 35 yr . This indicates that rapid intercompartment clearance $\left(\mathrm{V}_{1} \cdot \mathrm{~K}_{12}\right)$ decreases with increasing age. Age did not have a statistically significant effect on the rate constant $K_{13}$ that describes the distribution to the slowly equilibrating compartment (slow intercompartment clearance). The final model presented in table 2A includes an adjustment for the individual's weight on $V_{1}$ and CL, and an effect of age on $K_{12}$. There was no significant effect of alcohol intake or age on the initial distribution volume or clearance. All parameters were well estimated with relatively small standard errors. Interindividual variability (the variability in the data that can be assigned to different subjects) was assigned to four


Fig. 4. The individual thiopental serum concentration versus time curves in the 18 subjects aged greater than 60 yr during a thiopental infusion normalized to a rate of $100 \mathrm{mg} / \mathrm{min}$.
of the six model parameters and ranged from $50-76 \%$ for the rate constants $\mathrm{K}_{12}$ and $\mathrm{K}_{13}$ to $48 \%$ for the initial distribution volume and $30 \%$ for metabolic clearance.

When we attempted to characterize the 16 patients who received a bolus iv injection using a three-compartment pharmacokinetic model (fig. 2), we could not accurately estimate the initial distribution volume. The standard error of the initial distribution volume exceeded the value of the parameter. Inclusion of the iv infusion data with the iv bolus data reduced the standard error for the parameter, thus making it possible to use the three-compartment model. It was not possible to compare the pharmacokinetics between the bolus and infusion data for thiopental because the bolus iv pharmacokinetics could not be characterized separately with the three-compartment model and population data analysis.

Figures 2, 3, and 4 present the distribution phase data from the first 10 min after the iv bolus injection or during the $3-10 \mathrm{~min}$ iv infusion that was used in the one-compartment pharmacokinetic analysis. Figure 2 demonstrates the clear biexponential decay that would not be suitable for a one-compartment model and could not be characterized in the NONMEM analysis. The one-compartment model adequately characterized the thiopental infusion data of figures 3 and 4, table 2B presents the results of the data analysis. Patient weight did not affect the distribution volume (Vd) or elimination rate constant ( $\mathrm{K}_{\mathrm{e}}$ ), both of which were highly correlated. $\mathrm{K}_{\mathrm{e}}$ was found to decrease linearly after 35 yr from a value of $0.347 \mathrm{~min}^{-1}$ at age 35 to $0.226 \mathrm{~min}^{-1}$ at age 80 yr , a $34 \%$ reduction. Age did not effect Vd.

Figure 5 simulates the effect of age on thiopental serum concentrations from an infusion of $100 \mathrm{mg} / \mathrm{min}$ in $35-$ $\mathrm{yr}, 60-\mathrm{yr}$, and $80-\mathrm{yr}$-old subjects using the data of Table 2 B . The standard deviations of the predicted serum concentrations at the end of 10 min are indicated. If the therapeutic serum concentration needed to achieve adequate induction of anesthesia is approximately $40 \mu \mathrm{~g} /$ ml , the elderly patient would reach this threshold concentration at approximately 4 min , the middle-aged patient at 5 min , and the young patient at 8 min .

## Population Pharmacodynamic Analysis

Figures 6 and 7 indicate the spectral edge versus apparent thiopental effect-site concentration relationship estimated using the semiparametric pharmacodynamic modelling concept. An apparent effect-site concentration versus spectral edge curve is displayed for each subject. Figure 6 includes all of the data available for subjects less than 60 yr while figure 7 includes the data for those greater than 61 yr. Table 3 indicates the pharmacodynamic analysis obtained from this data. Using the semiparametric modelling approach, the rate constant of

Table 2A. Three Compartment Thiopental Population Pharmacokinetics*

| Final Mode | Parameters |
| :---: | :---: |
| Three-compartment model, six parameters <br> Proportional inter-/intraindividual error model <br> Random effects on CL, $\mathrm{V}_{1}, \mathrm{~K}_{12}, \mathrm{~K}_{13}$ <br> No covariance on random terms <br> Age effect on $\mathrm{K}_{12}$ <br> Weight effect on CL and $V_{1}$ <br> No effect of alcohol intake on $V_{1}$ or CL <br> No effect of age on $V_{1}$ or $K_{19}$ <br> Unable to characterize iv bolus data with the model | $\mathrm{Cl}=0.003071 \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~min}^{-1}$ <br> CL interindividual variability $\pm 30 \%$ <br> $\mathrm{V}_{1}=0.0790 \mathrm{l} / \mathrm{kg}$ <br> $V_{1}$ interindividual variability $\pm 48 \%$ <br> If age $<=35, \mathrm{~K}_{12}=0.48 \mathrm{~min}^{-1}$ <br> $\mathrm{K}_{12}$ interindividual variability $\pm 51 \%$ <br> If age $>35, \mathrm{~K}_{12}=0.48-(0.00288 \cdot($ Age 35$)) \mathrm{min}^{-1} *$ $\mathrm{K}_{21}=0.0787 \mathrm{~min}^{-1}$ $\mathrm{K}_{19}=0.107 \mathrm{~min}^{-1}$ <br> $\mathrm{K}_{19}$ interindividual variability $\pm 76 \%$ $\mathrm{K}_{31}=0.00389 \mathrm{~min}^{-1}$ <br> Residual error $\pm 24 \%$ |

Table 2B. One-Compartment Thiopental Population Pharmacokinetics, Infusion Data from 1-10 min $\dagger$

| Final Model | Parameters |
| :---: | :---: |
| One compartment model <br> Two parameters: <br> Vd (distribution volume) and <br> $\mathrm{K}_{\mathrm{c}}$, rate constant of drug removal <br> Proportional interindividual error model <br> Additive intraindividual error model <br> Covariance between Vd and $\mathrm{K}_{\mathrm{e}}$ <br> $\mathrm{K}_{\mathrm{e}}$ decreasing with age $>\mathbf{3 5}$ <br> No significant effect of age on Vd <br> No significant effect of weight on Vd and $\mathrm{K}_{\mathrm{c}}$ <br> Unable to characterize bolus iv data with this model | $\mathrm{Vd}=6.07 \mathrm{I}$ <br> Vd interindividual variability $\pm 35 \%$ <br> If age $<=35, \mathrm{~K}_{\mathrm{e}}=0.347 / \mathrm{min}$ <br> If age $>35, \mathrm{~K}_{\mathrm{c}}=0.347-\left(0.00268 \cdot(\right.$ Age 35$)$ ) $\mathrm{min}^{-1} *$ <br> $\mathrm{K}_{\mathrm{c}}$ interindividual variability $\pm 50 \%$ <br> Correlation coefficient between Vd and $\mathrm{K}_{\mathrm{e}}=-0.86$ |

* Sixty-four subjects, 2325 data points.
$\dagger$ Forty-eight subjects, 578 data points.
blood:brain equilibration ( $\mathrm{K}_{\mathrm{e} 0}$ ) was estimated to be (mean $\pm$ SD) $0.58 \pm 0.28 \mathrm{~min}^{-1}$. This corresponds to a $\mathrm{T}_{1 / 2} \mathrm{~K}_{\mathrm{e} 0}$ of $1.2 \mathrm{~min} . \mathrm{T}_{1 / 2} \mathrm{~K}_{\mathrm{e} 0}$ is linearly related to age with a slope that is statistically different than zero. However, the cor-


FIG. 5. The predicted thiopental serum concentration versus time curves for an infusion of $100 \mathrm{mg} / \mathrm{min}$ in subjects aged 80 yr (top curve), 60 yr (middle curve), and 35 yr (lower curve). The pharmacokinetic data from the one-compartment analysis of table 2 B was used. One standard deviation of the prediction is displayed for each curve at the end of the $10-\mathrm{min}$ infusion.
relation of age to $\mathrm{T}_{1 / 2} \mathrm{~K}_{\mathrm{e} 0}$ was extremely poor, with only $11 \%$ of the variability being explained by age. Although this relationship is statistically significant, we do not consider it to be clinically relevant. Table 3 presents a pharmacodynamic analysis of the spectral edge versus effect site concentration relationship. A sigmoid $\mathrm{E}_{\text {max }}$ pharmacodynamic model was found to be statistically preferable to the simpler $E_{\text {max }}$ model that does not include a power function $(\gamma)$. The pharmacodynamic parameters $\mathrm{E}_{0}$ (spectral edge [ Hz ] at maximal EEG activation), $\mathrm{E}_{\text {max }}$ (maximal decrease of the spectral edge $[\mathrm{Hz}]$ by thiopental), and $\mathrm{IC}_{50}$ (thiopental serum concentration $[\mu \mathrm{g} / \mathrm{ml}]$ at half of the maximal decrease ( $\mathrm{E}_{\text {max }}$ )) were estimated for the sigmoid $\mathrm{E}_{\text {max }}$ model with small standard errors. The interindividual variability assigned to the pharmacodynamics was moderate, ranging from $16-41 \%$. There was no effect of age on any of the pharmacodynamic parameters.

## Discussion

We have re-examined the effect of increasing human age on thiopental pharmacokinetics and pharmacodynamics. New data analysis techniques were applied to the data we have previously reported, using population analysis approaches and semiparametric pharmacodynamic


Apparent thiopental concentration at the effect site ( $\mu \mathrm{g} / \mathrm{ml}$ )

Fig. 6. The individual spectral edge versus apparent thiopental effect compartment concentration in 25 subjects aged less than 60 yr . Five subjects have two separate studies displayed. The semiparametric pharmacodynamic modelling approach was used to remove the disequilibrium from the measured thiopental concentrations versus spectral edge relationship.
modelling. We confirmed our previous report that age does not affect brain sensitivity to thiopental, using the EEG as a measure of CNS effect. The method of drug administration affected our ability to characterize thiopental's distribution phase with traditional pharmacokinetic models. When traditional pharmacokinetic models were applied to the data in subjects receiving an iv infusion of thiopental, an age-related effect on the rate of thiopental distribution from the central compartment was detected. However, the initial distribution volume could not


FIG. 7. The individual spectral edge versus apparent thiopental effect compartment concentrations in 13 subjects aged greater than 60 yr .
be characterized with the three-compartment pharmacokinetic model when thiopental was given by bolus iv injection.

In reanalyzing our pharmacodynamic data, we combined the thiopental serum concentration and spectral edge data from the previously reported studies of Homer and Stanski ${ }^{1}$ and Swerdlow et al. ${ }^{8}$ Using these two data sets and the additional subjects of the current study allowed for an increased group size, specifically in the young and middle-aged subjects. Collection and measurement of the thiopental serum concentrations, EEG recording, and waveform data analysis were performed in a uniform fashion in both studies. The reanalysis involved a new conceptual approach in relating thiopental serum concentrations to the spectral edge: semiparametric effect compartment modelling. ${ }^{5-7}$ This approach allows a more careful examination of the raw data by first removing the underlying disequilibrium in the relationship between thiopental serum concentrations and the spectral edge. One can then see the predicted effect site concentration versus spectral edge relationship without first applying an a priori pharmacodynamic model. Examining the raw data in figures 6 and 7, the apparent effect site concentration versus change in spectral edge relationship was similar in elderly and young subjects.
Having removed the disequilibrium from the thiopental serum concentration versus spectral edge data, it was possible to explore several alternative pharmacodynamic models using a population data analysis approach. We confirmed that the sigmoid $\mathrm{E}_{\text {max }}$ pharmacodynamic model provided the optimal characterization for this type of data. When three relevant parameters $\left(\mathrm{E}_{0}, \mathrm{E}_{\text {max }}\right.$, and $\left.\mathrm{IC}_{50}\right)$ were examined for age-related changes, no relationship could be detected. This confirms our previous finding that with increasing age, brain sensitivity to thiopental, as reflected by changes in the EEG, does not change. ${ }^{1}$

In the pharmacodynamic data, a subgroup of the subjects had a history of excessive alcohol intake. We included these subjects in the current data analysis because they had a thiopental dose requirement that was not statistically different from a control group who had only a "social" alcohol use history. ${ }^{8}$ Additionally, the parametric pharmacodynamic modelling demonstrated that "heavydrinking" subjects were not pharmacodynamically different from the control subjects. Removing these subjects from the data analysis did not change the conclusions of the pharmacodynamic analysis.

Complete understanding of the effect of increasing age on brain response to thiopental await the calibration of changes in the EEG to traditional clinical measures of thiopental depth of anesthesia. If the thiopental-induced changes in the EEG do correlate with clinical measures of anesthetic depth, our data predict that brain re-

Table 3. Thiopental Population Pharmacodynamics*

| Final Model | Parameters |
| :---: | :---: |
| Sigmoid $\mathrm{E}_{\text {max }}$ model $\text { Spectral edge }=\mathrm{Eo}-\frac{\mathrm{E}_{\max } \cdot \mathrm{Ce}^{\gamma}}{\mathrm{IC}_{50}{ }^{\gamma}+\mathrm{Ce}^{\gamma}}$ | $\mathbf{E}_{0}=23.0 \mathrm{~Hz}$ <br> Interindividual variability $\pm 16 \%$ <br> $\mathrm{E}_{\text {max }}=15.4 \mathrm{~Hz}$ <br> Interindividual variability $\pm 24 \%$ <br> $\mathrm{IC}_{50}=17.9 \mu \mathrm{~g} / \mathrm{ml}$ <br> Interindividual variability $\pm 41 \%$ $\gamma=2.72$ |
| No effect of age on $\mathrm{E}_{0}, \mathrm{E}_{\text {max }}, \mathrm{IG}_{50}$, or $\gamma$ <br> $\mathrm{K}_{\mathrm{c} 0}$ estimate for 38 subjects $=0.58 \pm 0.28 \mathrm{~min}^{-1}$ (mean $\pm$ SD) <br> Corresponding $\mathrm{T}^{1 / 2} \mathrm{~K}_{\mathrm{tc}}$ of 1.17 min <br> Linear regression of age versus $\mathrm{T} 1 / 2 \mathrm{~K}_{\mathrm{e} 0}$ significant but the coefficient of determination $\left(\mathrm{R}^{2}=0.11\right)$ was very low |  |

* Thirty-eight subjects, 1193 measured spectral edge versus predicted
sponsiveness to thiopental does not change with increasing age.

In our thiopental pharmacokinetic analysis, our population included a group of subjects who had a history of excessive alcohol consumption. Traditional data analysis using a two-stage approach had demonstrated that the thiopental serum concentration versus time profiles were not significantly different in the heavy drinkers versus the "social" drinkers who made up the control group. ${ }^{8}$ This finding confirmed a report by Couderc et al. ${ }^{12}$ who also did not find an effect of chronic alcoholism on thiopental distribution pharmacokinetics. With this finding, we included the heavy drinkers in our data analysis.

There are two major issues in our pharmacokinetic analysis of thiopental. The first issue involves the effects of age on thiopental pharmacokinetics. The second issue involves the ability of pharmacokinetic models to characterize distribution phase pharmacokinetics relative to the method of drug administration (iv bolus $v s$. rapid infusion). We found that, following bolus iv administration of thiopental to 16 patients and with blood sampling for up to 24-48 h, population pharmacokinetic data analysis could not accurately estimate the initial distribution volume using traditional pharmacokinetic models.

This experience with characterizing thiopental distribution pharmacokinetics is typical of the problem of using pharmacokinetic models for rapid distribution phenomenon. The traditional mammillary pharmacokinetic models have numerous assumptions. These include: 1) instantaneous mixing occurs in the central compartment; 2) the pharmacokinetics are stationary (i.e., volumes and clearances do not vary over time); and 3) blood samples are obtained instantaneously from the central compartment. All of these assumptions are likely to be violated during the initial distribution/phase of thiopental. Crankshaw et al. ${ }^{13}$ examined the short-term distribution of thiopental in the dog, using iv bolus injections administered over 5-
effect compartment concentration data points, five subjects had two separate studies.

30 s. Frequent arterial serum concentrations were obtained at $3-5$-s intervals over the first minute. They demonstrated that the peak thiopental concentrations do not occur instantaneously and will vary with the duration of injection time. There was significant variability in the peak concentrations achieved and in the rate of decline. The plots of time versus concentration were described as having a shape that would be anticipated for the dispersion of a rapidly administered bolus into a fast-moving circulation. The leading edges were steep while the tails are extended, suggesting some transient uptake by the pulmonary tissues. There is little evidence of recirculation, indicating a high degree of distribution into the richly perfused tissues. Crawford ${ }^{14}$ took a more empirical anatomic and physiological approach to describing the initial distribution of injected iv bolus doses. He indicated the multiple factors governing the peak transients that occur with rapid versus slow iv administration of drugs. Niazi has shown, in a theoretical comparison of zero-order input relative to the generally accepted instantaneous intravascular input, that it is not possible to assume that mixing will occur instantancously in mammillary pharmacokinetic models. ${ }^{15}$ The assumption of instantaneous mixing will always result in an error, but this error can be corrected if the data is treated as an intravascular administration of a zero-order infusion. He recommends that all inputs be modelled as zero-input into two- and three-compartment open pharmacokinetic models. Bischoff and Brown have also created a detailed physiological model that breaks the body down into multiple small compartments, called the "minimammal." ${ }^{16}$ They again demonstrate that there are multiple transients throughout different portions of the body when physiological models are used to predict drug concentrations over time during the initial distribution within the body. Thus it is no surprise that our attempt to use traditional pharmacokinetic models to characterize the initial distribution volume over a large group of patients using
frequent arterial sampling was not successful. Henthorn et al. ${ }^{17}$ have simultaneously administered thiopental and an additional intravascular indicator, indocyanine green (ICG). They have proposed simultaneous modelling of ICG with the thiopental concentration decay that results in thiopental distribution phase pharmacokinetic parameters with more physiological constraints. Their results suggest that a 2-3 min "mixing phase" occurs during thiopental distribution. The more sophisticated pharmacokinetic modelling proposed by Henthorn et al. has significant promise to characterize drug distribution pharmacokinetics.

Our one-compartment analysis represents an approach of simplifying the pharmacokinetic modelling to the data maximally relevant to the clinical drug effect. For thiopental this represents the first $10-15 \mathrm{~min}$ following drug administration. The one-compartment modelling demonstrated that aging changes the rate of thiopental elimination in the first few minutes of drug administration and confirmed the results of the complete three-compartment modelling.

The issue of distribution pharmacokinetics for thiopental has been further confused in the literature by arterial/venous sampling differences. Numerous thiopental pharmacokinetic studies have used peripheral venous sites to sample the initial serum concentrations. ${ }^{18-22}$ There is a large body of literature that demonstrates significant differences between the arterial and venous drug concentrations for most drugs, including thiopental. Barrett et al. ${ }^{23,24}$ have demonstrated in both animals and man that thiopental concentrations from venous sites reach a peak up to 2 min after completion of the iv bolus injection. There was also a large intraindividual variability in the serum concentration versus time relationships when peripheral venous samples were used. Concentration differences between arterial and peripheral sampling sites were considerable in most subjects and averaged nearly $10 \%$, up to 9 min after bolus iv administration. Chiou et al. have confirmed the significance of arterial/venous concentration differences impacting on pharmacokinetics. ${ }^{25-29}$ Based upon their observation that the marked variation in initial distribution volume parameters is frequently proportional to the interval of sampling, they recommend that short iv infusions, rather than bolus iv injections, should be the preferred route for pharmacokinetic studies. The short iv infusion allows time for multiple blood samples to be drawn that will estimate the initial distribution phase. With an iv bolus, only one or two samples can be obtained to estimate the early distribution phase.

All compartmental pharmacokinetic models are based on the assumption that the parameters such as clearance and volume of distribution are constant over time, but there are several factors that might violate this assumption
and alter drug distribution and elimination. For a drug such as thiopental, which is dependant on cardiac output for its distribution, any drug-induced change in cardiac output might change the distribution phase pharmacokinetics. Additionally, clinically relevant noxious stimuli (i.e., laryngoscopy and intubation) can also cause profound changes in cardiovascular function, which might cause moderate changes in the rate and degree of the drug distribution. Many studies do not carefully specify whether perioperative stimuli were applied or the degree of hemodynamic response to the drug or the stimuli.

Our own approach to characterizing distribution pharmacokinetics has involved the use of a rapid iv infusion, with arterial serum concentration sampling at frequent intervals. Typically, one can obtain six to eight serum concentrations at half-minute intervals during the infusion and an equivalent number of serum concentrations during the first $3-5 \mathrm{~min}$ after termination of the infusion. The slower administration relative to the bolus injection tends to minimize unwanted side effects, i.e., hemodynamic and respiratory depression. This should, in principle, minimize the concern of nonstationary drug kinetics. Using this approach, it is possible to obtain 12-14 data points that can then be used to characterize rapid and slow distribution phase components. These 12-14 data points are more than adequate for the estimation of the pharmacokinetic parameters (initial distribution volume, rapid and slow intercompartment clearances, metabolic clearance) that characterize the distribution phase. The data analysis in this study demonstrates that it is possible to obtain consistent and reliable pharmacokinetic data, using a rapid iv infusion with frequent arterial blood sampling. This is also compatible with the suggestions of many other theoretical and experimental studies regarding characterization of distribution phase kinetics. We would thus not recommend bolus iv injections for drug administration in pharmacokinetic studies where the distribution pharmacokinetics are of relevance and traditional pharmacokinetic modelling approaches are to be used.

In our previous publication, ${ }^{1}$ the mode of drug administration was both iv bolus injection and rapid iv infusion. The younger subjects received an iv bolus injection, while the middle-aged and older received a rapid iv infusion. The initial distribution volumes estimated from the iv bolus studies were significantly larger, i.e., 15-20 1/70kg subject, compared with the initial distribution volumes estimated in the middle-aged to elderly subjects, 3-10 $1 / 70 \mathrm{~kg}$. The age-related change in initial distribution volume we previously reported may reflect a methodological artifact from using bolus iv and infusion data interchangeably. Also, the previously discussed inaccuracy of distribution phase pharmacokinetics obtained from rapid iv bolus dosing could also explain our previous data.

With this in mind, we have reanalyzed our data in an attempt to characterize properly the effect of age on thiopental distribution pharmacokinetics.

We have demonstrated that with increasing age there is a change of thiopental's rapid intercompartment clearance while the initial distribution volume did not change with age. Following a rapid iv bolus, the peak thiopental serum concentrations that occur within $15-30 \mathrm{~s}$ will be similar in the young and elderly patients because the initial distribution volume is not altered by aging. After the peak serum concentration is achieved, two pharmacokinetic factors will serve to decrease the serum concentrations: rapid and slow intercompartment clearance that represents distribution of drug into highly perfused and less well-perfused tissues, and hepatic metabolism of the drug. Thiopental serum concentrations will not decrease as rapidly in the elderly versus young patient because the rapid intercompartment clearance is lower in the elderly patient. The higher thiopental serum concentrations that occur in the minutes after the iv bolus will result in more thiopental being available for distribution into the biophase (brain) to create a greater anesthetic effect in the elderly. Our pharmacokinetic analysis indicates that the rapid intercompartment clearance is approximately $30 \%$ lower in the elderly ( 80 yr ) versus young patient. Examining the raw serum concentration versus time data during the infusion of thiopental (figs. 3 and 4) one can see that the elderly subjects are consistently in the upper border of the thiopental serum concentrations relative to young and middle-aged subjects.

Using NONMEM for population pharmacokinetic data analysis, we found that the distribution pharmacokinetic parameters had significantly higher variability compared with the elimination phase parameters (i.e., metabolic clearance). Given that thiopental distribution pharmacokinetics are dependant on cardiovascular function, specifically perfusion, the variability in cardiac function and cardiac output might explain in part the $30-70 \%$ variability in thiopental distribution pharmacokinetic parameters. Our ability to individualize thiopental administration will therefore be dependent upon obtaining noninvasive measures of the patient's physiological cardiovascular function prior to the administration of thiopental. At present there are no practical mechanisms for this.

In summary, we have re-examined the effect of age on thiopental pharmacokinetics and pharmacodynamics in humans. We found that iv bolus administration of thiopental did not allow accurate characterization of thiopental distribution phenomenon. Using a rapid iv infusion, we demonstrated that increasing age decreased thiopental rapid intercompartment clearance. Initial distribution volume was not age related as we previously have re-
ported. Thiopental EEG pharmacodynamics are not altered with increasing age.

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[^1]:    Sources: *Homer and Stanski. ${ }^{1} \dagger$ Swerdlow et al. ${ }^{8} \ddagger$ Present study.

[^2]:    $\ddagger$ Beal SL, Sheiner LB: NONMEM User's Guide, San Francisco, University of California, 1979
    § Run on a Unix V/3 operating system with an Opus PM 350 addin board in a generic AT-286 clone.

